



TransCom, San Francisco, 1998

# Atmospheric Inversions

Estimating fluxes of carbon dioxide and other greenhouse gases

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17 March 2015

OCEANS AND ATMOSPHERE FLAGSHIP

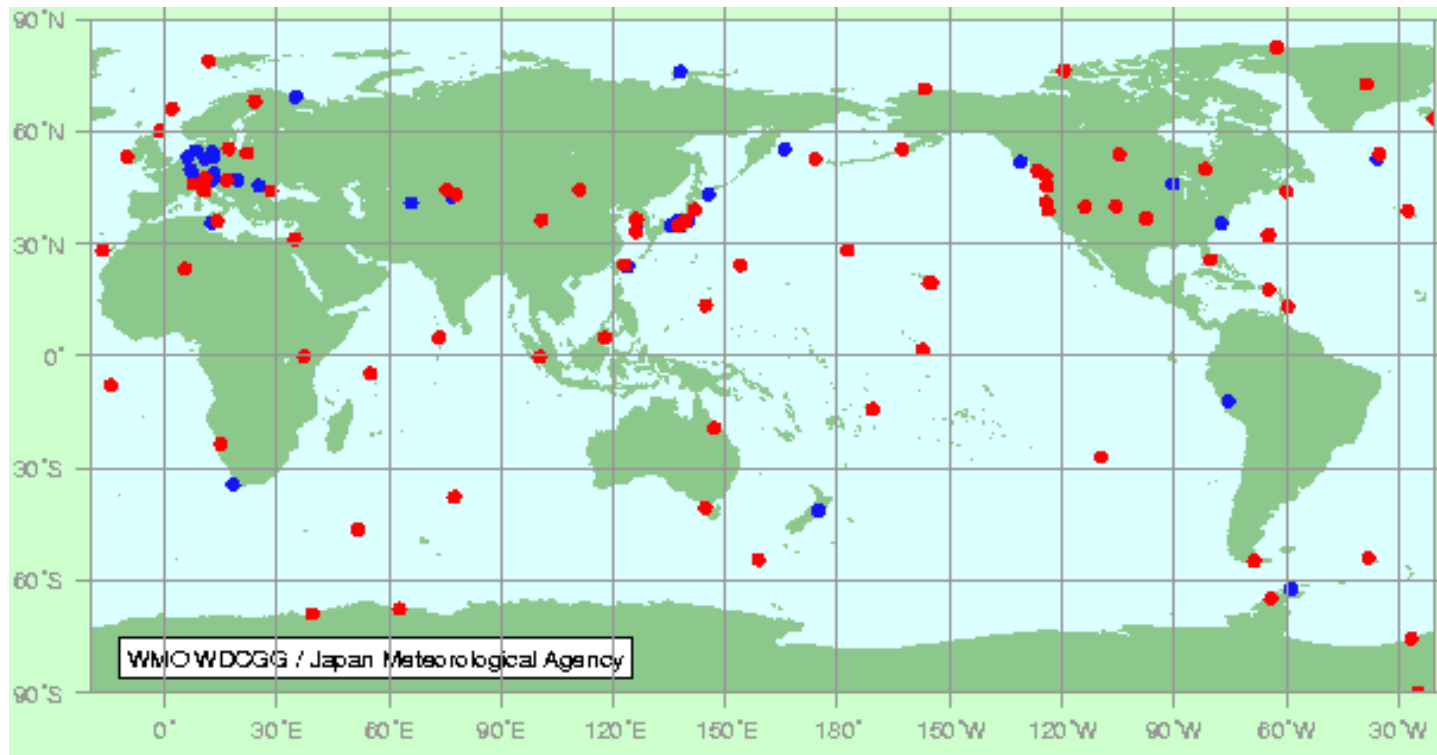
[www.csiro.au](http://www.csiro.au)



# Atmospheric measurements of CO<sub>2</sub>

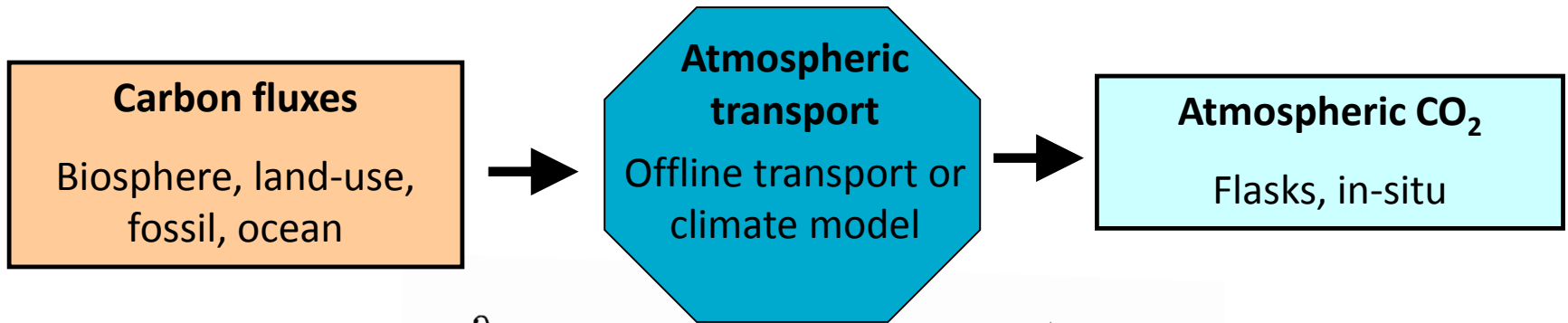
World Data Centre for Greenhouse Gases

<http://gaw.kishou.go.jp/wdcgg/>

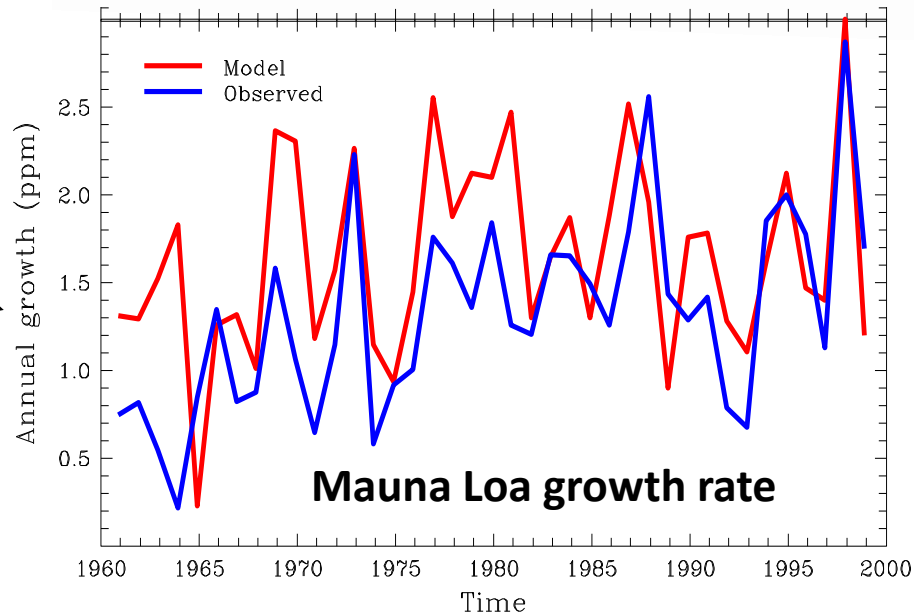


Network biased to remote, clean-air conditions.  
Many marine boundary layer or mountains.

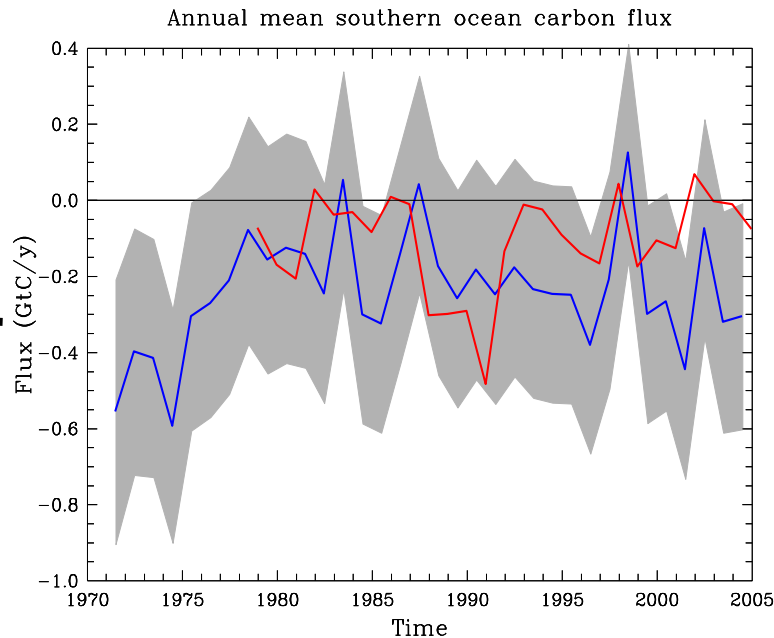
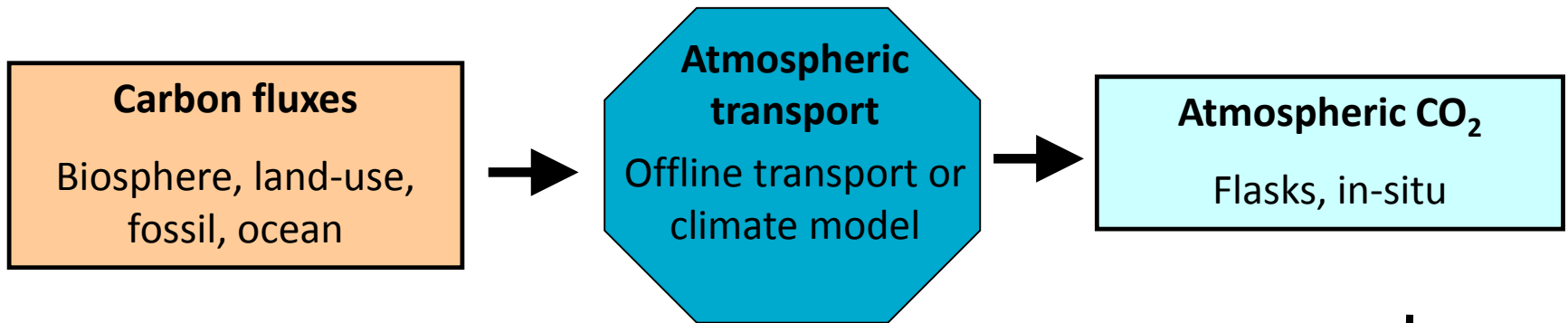
# Transport links fluxes and mixing ratios



$$\frac{\partial}{\partial t} m(\mathbf{r}, t) = s(\mathbf{r}, t) + \mathcal{T}[m(\mathbf{r}, t), t] \quad (1.2.1)$$



# Transport links fluxes and mixing ratios



# Inversion timeline – Ian's contributions

## 1985

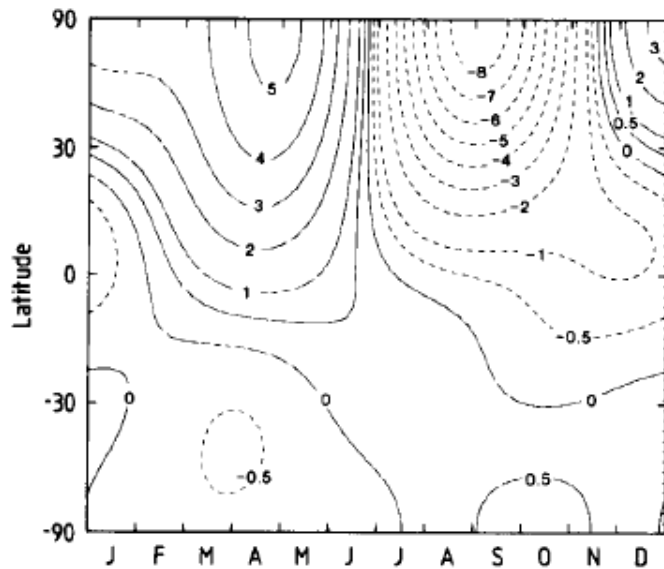
- Principles of Constrained Inversion in the Calibration of Carbon-Cycle Models, *Tellus*, 37B.
- Green-Functions and response functions in geochemical modeling, *Pure and Applied Geophysics*, 123.
- A Classification of some inverse problems in geochemical modeling, *Tellus*, 37B.

## 1988-1993

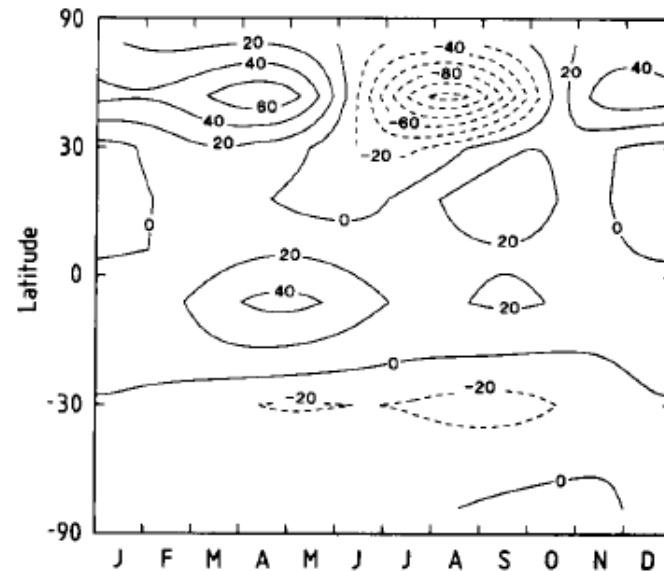
- Inversion problems in atmospheric constituent studies, *Inverse Problems*
  - Newsam and Enting, 1. Determination of surface sources under a diffusive transport approximation (1988)
  - Enting and Newsam, 2. Sources in the free atmosphere (1990)
  - Enting, 3. Estimating errors in surface sources (1993)

# Applications (1)

Enting and Mansbridge, Seasonal sources and sinks of atmospheric CO<sub>2</sub>: Direct inversion of filtered data, Tellus, 41B, 1989



CO<sub>2</sub> concentration



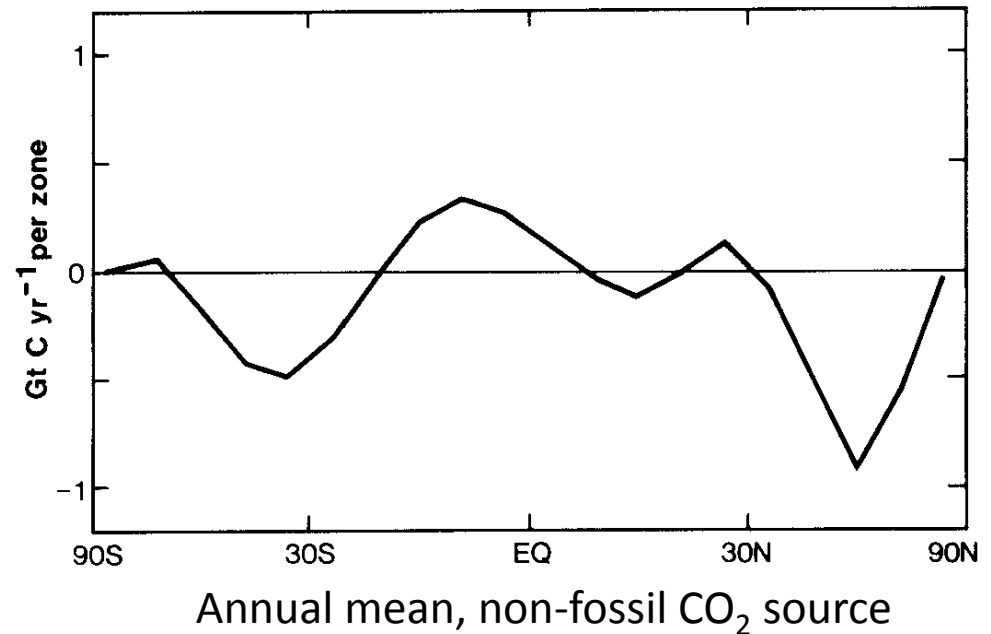
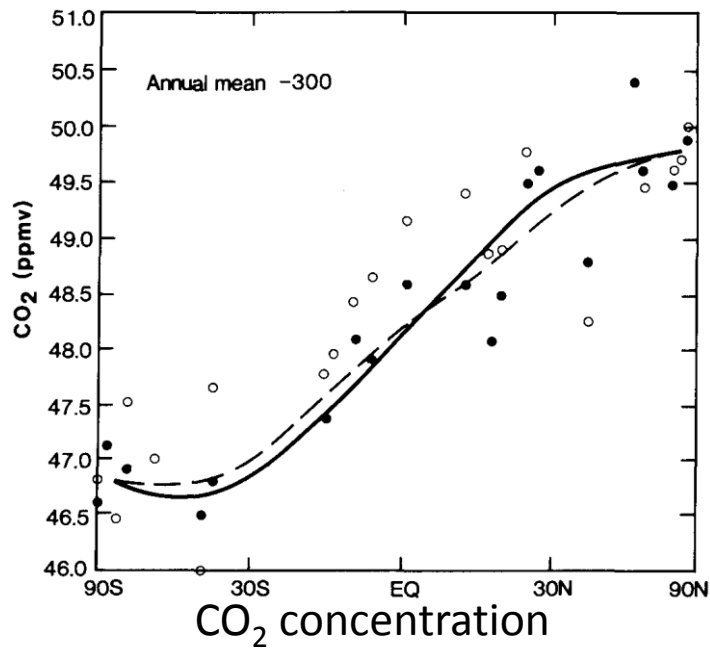
CO<sub>2</sub> source

2d transport model. Interpretation of annual mean and seasonality.

71 citations

# Applications (2)

Enting and Mansbridge, Latitudinal distribution of sources and sinks of CO<sub>2</sub> – results of an inversion study, Tellus, 43B, 1991



Inclusion of CO, 2d transport model  
97 citations

# Applications (3)

Enting, Trudinger and Francey, A synthesis inversion of the concentration and  $\delta^{13}\text{C}$  of atmospheric  $\text{CO}_2$ , Tellus, 47B, 1995

Presented at 4<sup>th</sup> International  $\text{CO}_2$  conference, Carqueiranne, France, 1993

3d transport

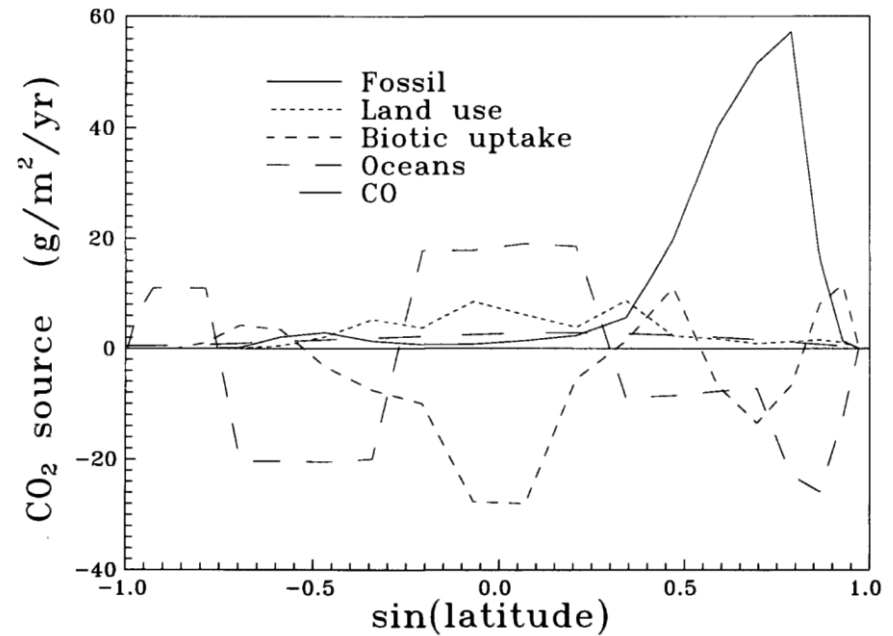
$\text{CO}_2$  isotope – to help distinguish land and ocean sources

Uncertainties

1986-1987 compared to 1989-1990

Limits of quasi-steady state?

235 citations







**ANNUAL  
REPORT  
1993-1994**

**Program B - Global Transport  
Modelling**

**Objective**

To improve the scientific basis for the atmospheric transport modelling used in Australia for input to environmental policy on issues such as greenhouse gas emissions. This requires the development of a versatile 3-D transport model and improved inversion methodologies to infer trace gas sources.

**Research Staff**

I Enting, R Francey, P Fraser, R Law, L P Steele,  
I Watterson.



*Dr Ian Enting, Program Leader*



Tom Wilely, Office for Interdisciplinary Earth Science

*Dr Ian Enting, Program Leader*

November 1993: 2<sup>nd</sup> Workshop on Inverse Modelling Problems in Atmospheric Constituent Transport (WIMPACT-2)

August 1994: Peter Rayner joins CRCSHM

1994-1998: TransCom coordination

1995/1996: Ian leads 'B2: Greenhouse Gases'

# Applications (4)

Rayner, Enting, Francey and Langenfelds, Reconstructing the recent carbon cycle from atmospheric CO<sub>2</sub>, δ<sup>13</sup>C and O<sub>2</sub>/N<sub>2</sub> observations, Tellus, 51B, 1999

Presented at 5<sup>th</sup> International CO<sub>2</sub> conference, Cairns, Australia, 1997

3d transport  
CO<sub>2</sub> isotope and oxygen – to help distinguish land and ocean sources

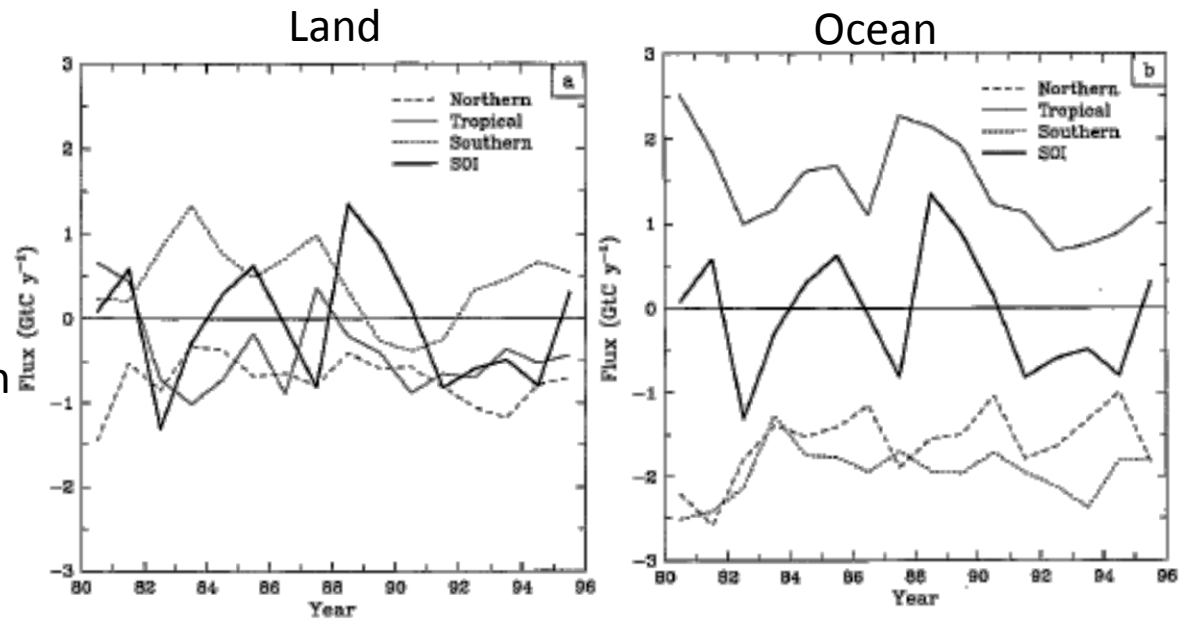
Uncertainties

Time-dependent, 1980-1995

Bayesian synthesis inversion

ENSO, Pinatubo

287 citations



# Education

## Workshops

- Symposium Workshop on Inverse Modeling of Global Biogeochemical Cycles, Iraklion, Greece, 1998
- Enting, Green's function methods of tracer inversion
- In 'Inverse Methods in Global Biogeochemical Cycles', Geophysical Monograph Series, 114, 19-31, 2000

## The book

- IG Enting, Inverse Problems in Atmospheric Constituent Transport, Cambridge University Press, 2002 (164 citations)

# TransCom (Transport Comparison)

1993 CO<sub>2</sub> conference

- Forward simulations, CO<sub>2</sub> fossil and biosphere, SF<sub>6</sub>

1997 CO<sub>2</sub> conference

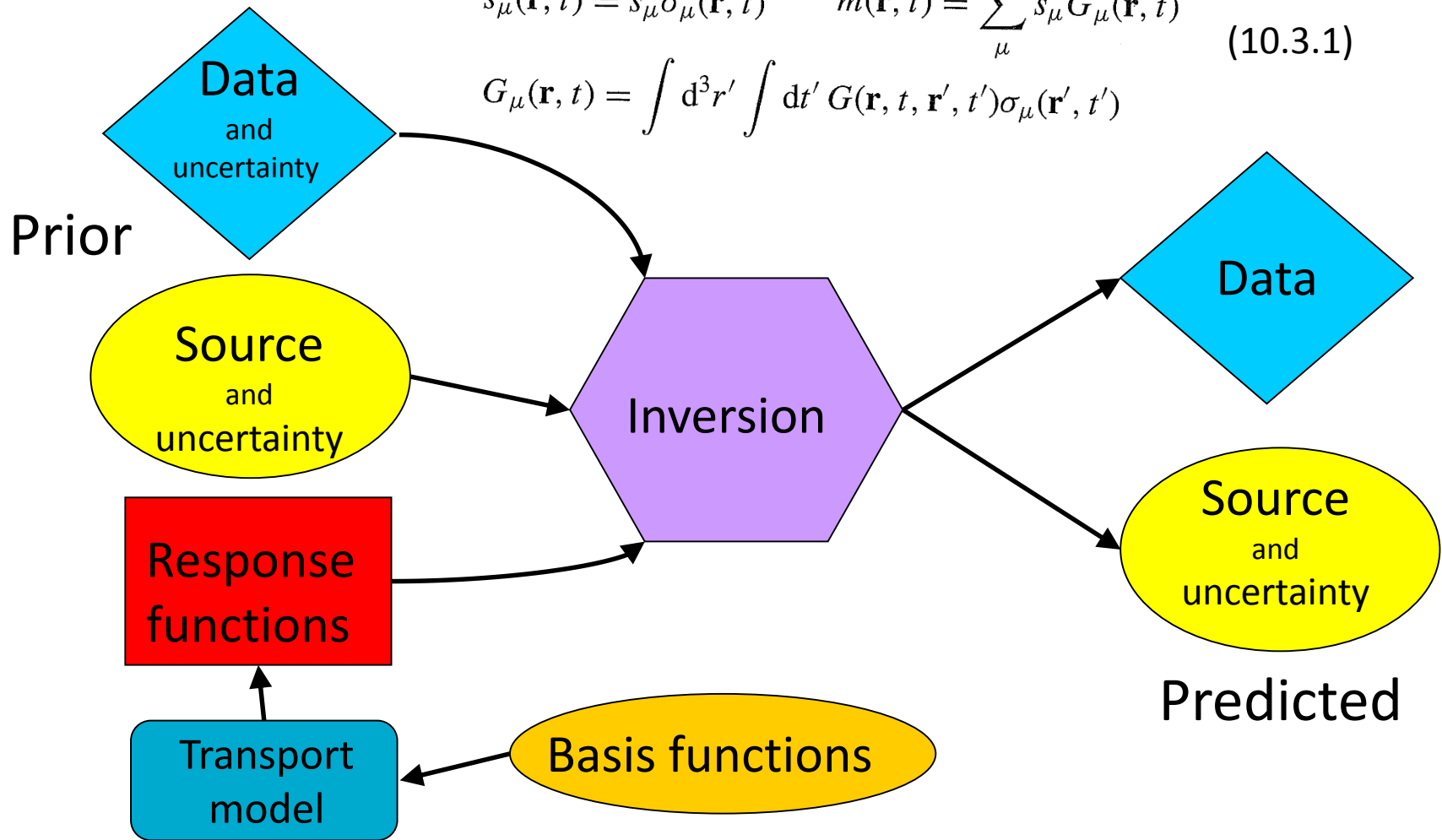
- Inversions
- Scott Denning, NSF Grant, funding for coordination and workshops
- Feb 1998, Santa Barbara planning meeting  
(Australian vs GFDL proposals, global vs N American focus)
- Dec 1998, San Francisco, kick-off meeting



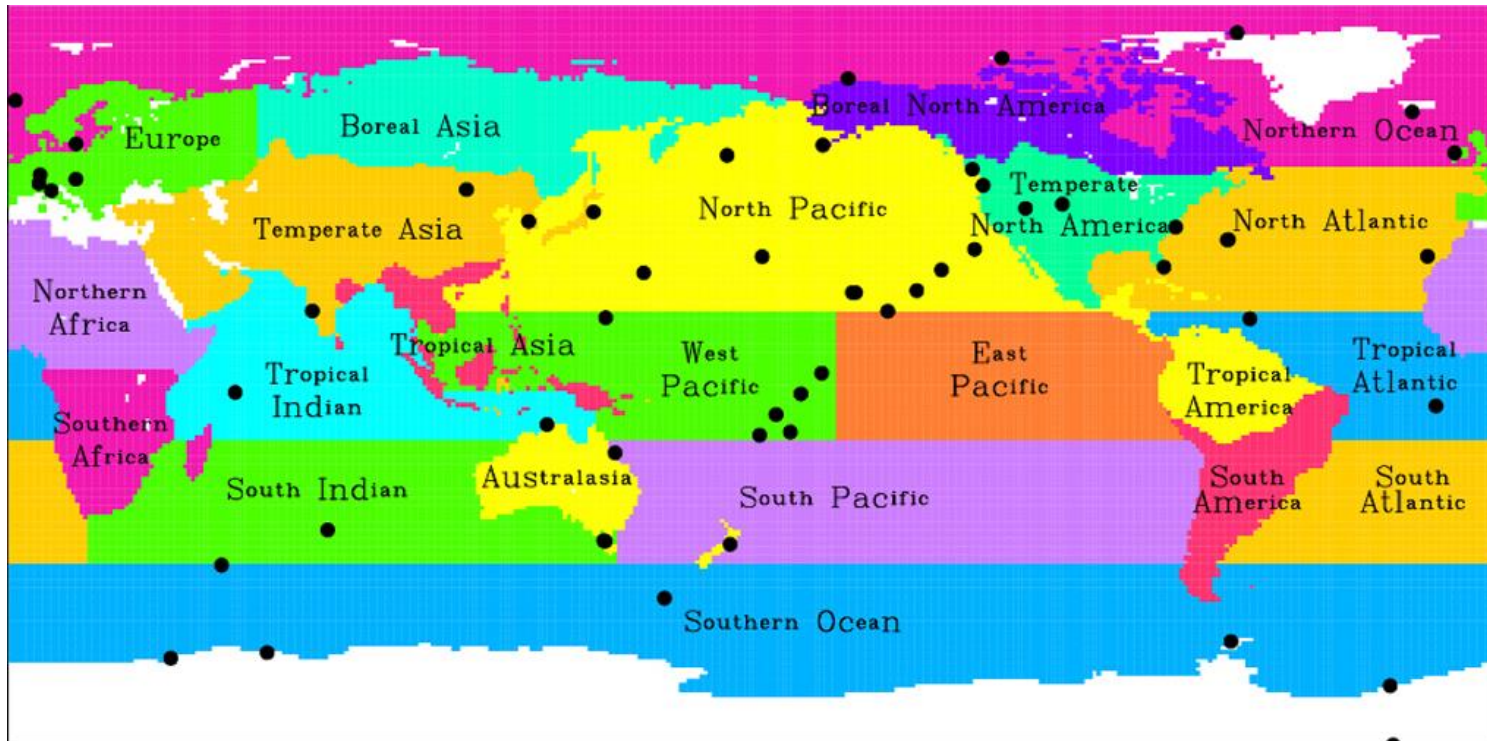
# Bayesian synthesis inversion

$$s_\mu(\mathbf{r}, t) = s_\mu \sigma_\mu(\mathbf{r}, t) \quad m(\mathbf{r}, t) = \sum_\mu s_\mu G_\mu(\mathbf{r}, t) \quad (10.3.1)$$

$$G_\mu(\mathbf{r}, t) = \int d^3r' \int dt' G(\mathbf{r}, t, \mathbf{r}', t') \sigma_\mu(\mathbf{r}', t')$$



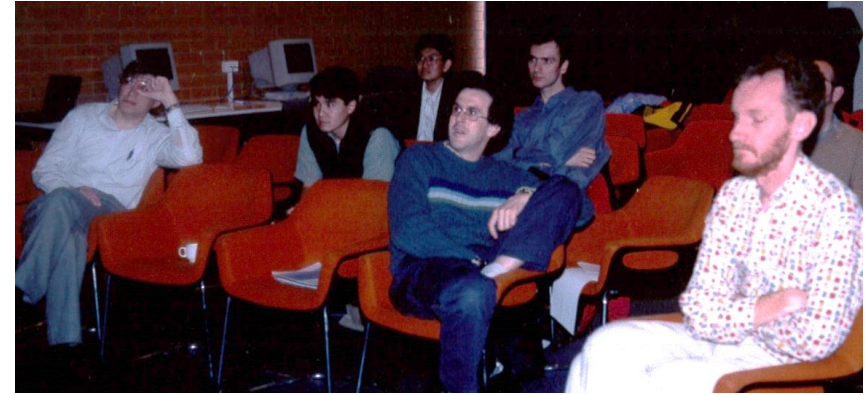
# TransCom regions / Basis functions



Background fluxes: fossil fuel, neutral biosphere - 'rectifier', air-sea exchange.

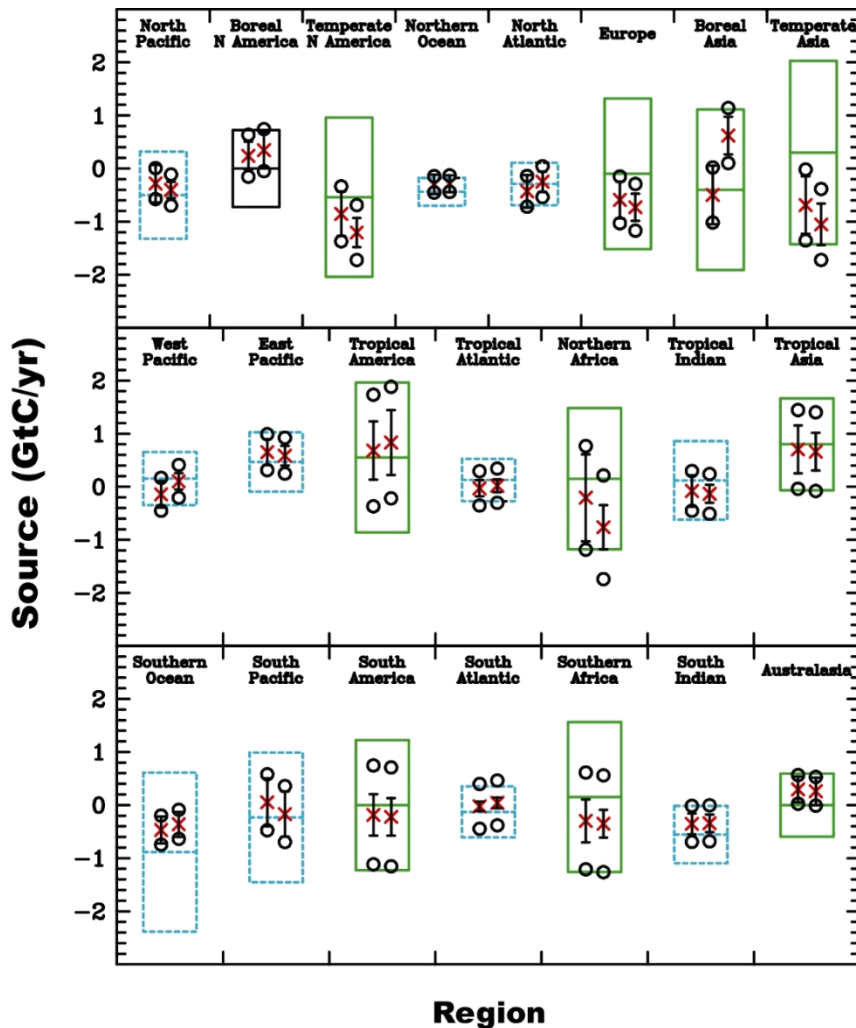
# TransCom, Melbourne 2001

“Work on finalizing the Science paper was completed. This contains the annual mean, level 1, control results from the experiment. We are about to submit to Science.”



“Many thanks to Ian Enting for hosting a wonderful get together at his home.”

# TransCom annual mean inversion (1992-1996)



Gurney et al, Nature, 2002, (572)

+ more detail, Tellus, 2003 (154, 42)

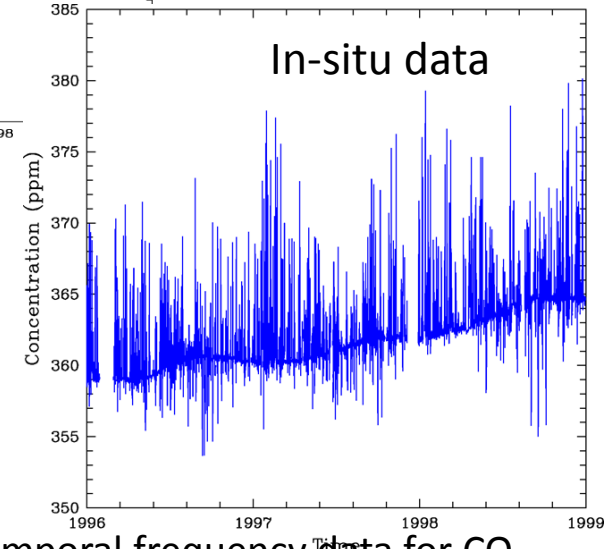
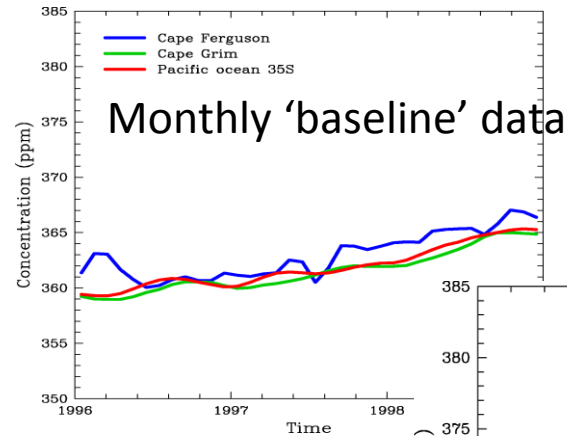
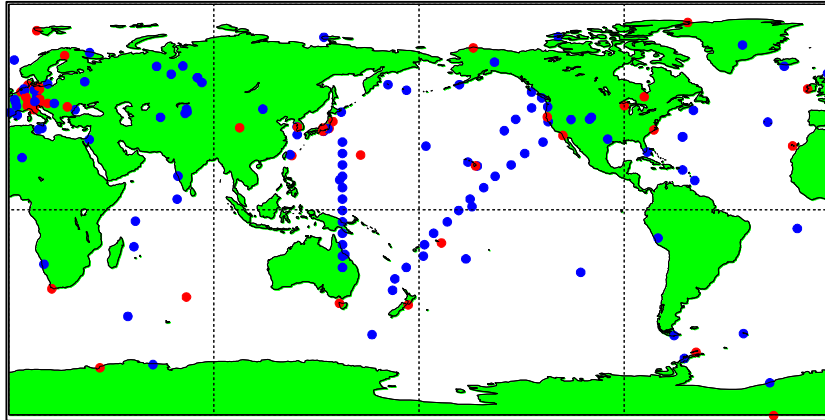
Seasonal cycle: Gurney et al, Tellus, 2004 (162)

Interannual: Baker et al, GBC, 2006 (69)

Model spread (error bar) mostly similar to predicted uncertainty (determined by data availability and uncertainty)

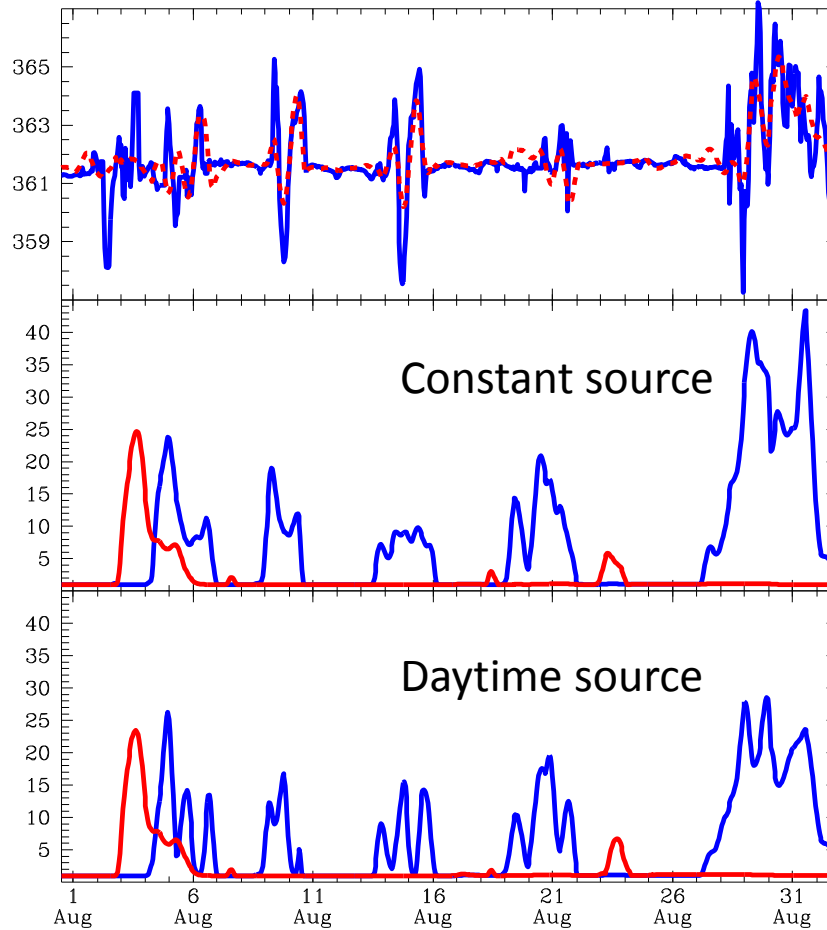


# Making use of in-situ sites with hourly data



- Law, R.M., P.J. Rayner, L.P. Steele and **I.G. Enting**, 2002: Using high temporal frequency data for CO<sub>2</sub> inversions, *Global Biogeochem. Cycles*, 16(4). 1053. doi:10.1029/2001GB001593.
- Law, R.M., P.J. Rayner, L.P. Steele and **I.G. Enting**, 2003: Data and modelling requirements for CO<sub>2</sub> inversions using high frequency data, *Tellus*, 55B, 512-521, doi:10.1034/j.1600-0560.2003.29.x.
- **Synthetic data**

# Real data – transport model limitations



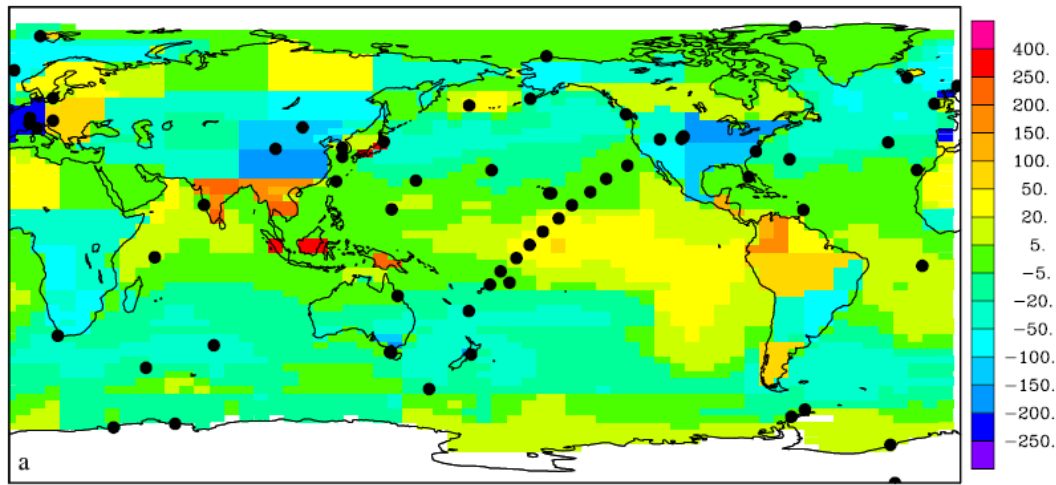
Blue – data

Red – inversion fit

Model responses

Blue – SE Australia

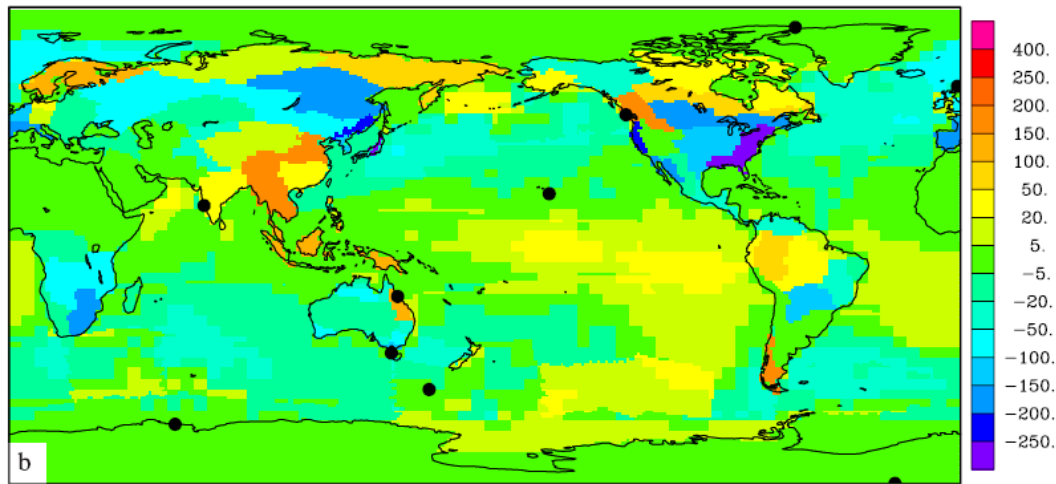
Red - Tasmania



Rayner et al., GBC, 2009  
 Bayesian synthesis (matrix) inversion  
 set up similarly to T3 (Baker et al.,  
 2006)

MATCH

67 land regions, 49 ocean regions



CCAM

94 land regions, 52 ocean regions

1992-2005 mean flux, colour boundaries on land  
 indicate typical region size

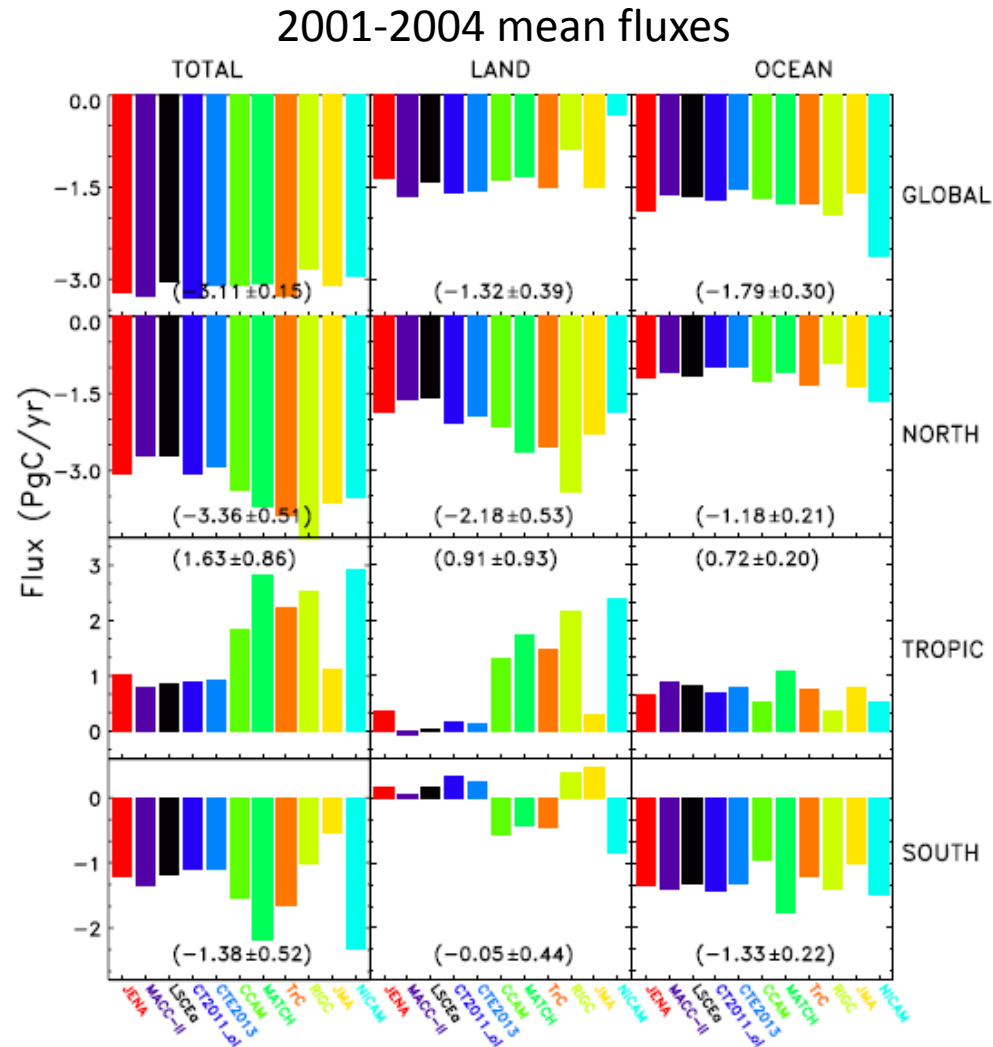
- 67 CO<sub>2</sub> sites
- 10 <sup>13</sup>C sites



# REgional Carbon Cycle Assessment and Processes (RECCAP)

Peylin et al., Global atmospheric carbon budget: results from an ensemble of atmospheric CO<sub>2</sub> inversions, Biogeosciences, 2013.

- Multiple inversion methods
- Monthly mean data or flasks/in-situ at observing time (mid-afternoon only)



# Enting et al: Carbon Cycle Uncertainty in RECCAP (Biogeosciences, 2012)

Inversions represent cases of indirect inference where the direction of inference is in the opposite direction to real-world causality. Consequently, the dissipative nature of most biophysical systems means that such inverse problems will be ill-conditioned: highly sensitive to both model error and data error.

The RECCAP study is a unique effort in synthesising a large body of quantitative knowledge about the carbon cycle. Experience from comparable exercises in other contexts suggest that as much will be learned about the problems in performing such an exercise for the first time as is learned about the targeted science. Examples from our own experience include:

- The Transcom intercomparison, where initial compromises (e.g. the neglect of reduced carbon, fossil emissions either fixed or with a single global uncertainty) have persisted;

# Thank you

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